

## Blurbs for Cart Lab

1.) Velocity of cart at  $t = 0.5$  sec.:

- a.) using *velocity vs time* graph
- b.) using *position vs time* graph
- c.) determine  $v_{.5}$  using  $v_2 = v_1 + a(\Delta t)$  and graphs
- d.) determine  $v_{.5}$  using  $v_2^2 = v_1^2 + 2a\Delta x$  and graphs

2.) Distance traveled between  $t = 0.25$  and  $t = 0.60$  seconds.:

- a.) using *position vs time* graph
- b.) using *velocity vs time* graph
- c.) using  $x_2 = x_1 + v_1 t + .5at^2$  and data from graphs

3.) determine % deviation for largest value discrepancy using information from:

- a.) Question 1 (determining final velocity)
- b.) Question 2 (distance traveled)

Questions:

1. What is the velocity of the cart at  $t=0.5\text{s}$ ?

a) ... using the velocity-time graph

$$V(0.5) \approx +1.13 \text{ m/s}$$

we found this velocity by looking at the velocity time graph to see the y-coordinate of the point at  $0.5\text{s}$ . Then, we confirmed our estimate by using the equation for the best fit line ( $y = 1.542x + 0.3612$ ).

b) ... using the distance-time graph

$V(0.5) \approx +1.39 \text{ m/s}$  we found this value by approximating the slope of the graph at  $t=0.5\text{s}$ . Then, we confirmed our estimate by using the derivative of the best fit line for the graph, which was  $y = -0.009771x^2 + 1.396x - 0.2710$  @  $t=0.5\text{s}$ .

c) ... using  $V_2 = V_1 + a\Delta t$

$$V_{0.5} = (0.45 \text{ m/s}) + (1.542 \text{ m/s}^2)(0.5\text{s} - 0.06\text{s})$$

$$V_{0.5} = +1.13 \text{ m/s}$$

Values used:  $t=0.06$ ,  $V=0.45 \text{ m/s}$ ,  $a=1.542 \text{ m/s}^2$

d) ... using  $V_2^2 = V_1^2 + 2a\Delta x$

$$V_{0.5}^2 = (0.45 \text{ m/s})^2 + 2(1.542 \text{ m/s}^2)(0.425\text{m} - 0.015\text{m})$$

$$V_{0.5} = +1.20 \text{ m/s}$$

Values used:  $@t=0.06\text{s}, V=0.45 \text{ m/s}, a=1.542 \text{ m/s}^2, d=0.015\text{m}$   
 $@t=0.5, d=0.425\text{m}$

2. How far did the hanging mass travel between  $0.25\text{s}$  and  $0.6\text{s}$ ?

a) find  $\Delta x$  using the distance-time graph  
using the equation of the line of best fit, we plugged in  $t=0.25$  and  $t=0.6$  to find that  $\Delta x = 0.486\text{m}$

$$y = -0.0971x^2 + 1.396x - 0.2710$$
$$@ t=0.25, x=0.077\text{m}$$
$$@ t=0.6, x=0.563\text{m}$$
$$\rightarrow 0.563 - 0.077 = 0.486\text{m}$$

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c.  $V_{0.5}$  using  $V_f = V_i + a \Delta t$

$$V = mt + b$$

$$V = [0.8771 \text{ m/s/s}] [0.030324] + [0.2770 \text{ m/s}]$$

$$V_{0.030324} = 0.304 \text{ m/s} \quad \text{finding } V_i$$

$$V = mt + b$$

$$\bar{a} = \frac{V_f - V_i}{T_f - T_i} \quad \text{acceleration is the slope of the velocity graph because it is the derivative}$$

$$\Delta t = 0.522283 - 0.030324 = 0.491959$$

first and last data pts

$$V_{0.5} = [0.304 \text{ m/s}] + [0.8771 \text{ m/s/s}] [0.491959 \text{ s}]$$

$$\boxed{V_{0.5} = 0.735 \text{ m/s}}$$

d.  $V_{0.5}$  using  $V^2 = V_i^2 + 2a \Delta x$

$$\Delta x = 0.255 \rightarrow \text{last point on distance-time graph}$$

$$V_{0.5}^2 = [0.304 \text{ m/s}]^2 + 2[0.8771 \text{ m/s/s}] [0.255 \text{ m}]$$

$$V_{0.5}^2 = 0.539$$

$$\boxed{V_{0.5} = 0.735 \text{ m/s}} \quad \text{took the square root}$$

2. How far did hanging mass travel between  $t = 0.25 \text{ s}$  and  $t = 0.6 \text{ s}$ ?

a.  $\Delta x$  using distance-time graph

because an equation is given, it tells us the velocity and distance

$$D = At^2 + Bt + C$$

$$D = [0.3116][0.25]^2 + [0.4001][0.25] + [-0.03012]$$

$$D_{0.25} = 0.089 \text{ m}$$

plugging into equation

$$D = [0.3116][0.6]^2 + [0.4001][0.6] + [-0.03012]$$

$$D_0 = 13.59 \text{ m}$$

$$D_0 - D_{0.25} = 13.59 - 0.089 = 13.50 \text{ m}$$

$$0.322 \rightarrow \boxed{0.233 \text{ m}}$$

Calculations

b. velocity at  $t=5s$ ?

a. Net v<sub>s</sub> using vel-time graph

$$v = 1271t + .04269 \quad \begin{matrix} \text{equation of line of} \\ \text{best fit for} \\ \text{velocity} \end{matrix}$$
$$.1271(5) + .04269 \quad \begin{matrix} \text{plug in time} \\ (.10624 \text{ m/s}) \end{matrix}$$

b. Net v<sub>s</sub> using dist-time graph

$$d = .86302t^2 + .04407t + .004371 \quad \begin{matrix} \text{take derivative of} \\ \text{distance line} \end{matrix}$$
$$.12604t + .04407 \quad \begin{matrix} \text{of best fit} \\ \text{plug in time} \end{matrix}$$
$$.12604(5) + .04407 \quad (.10704 \text{ m/s})$$

c. using ~~graph~~  $v_2 = v_1 + a\Delta t$

$$v = 1271t + .04269 \quad \begin{matrix} \text{take } \frac{dy}{dt} \\ \text{get acceleration} \end{matrix}$$
$$a = .1271$$

$$\text{At } t = .30919, \quad v_2 = .0872 + .1271(.19081)$$
$$v_1 = .0872$$

$$a = .1271$$
$$\Delta t = .5 - .30919 = .19081$$
$$v_s = .11145 \text{ m/s}$$

For the initial velocity, I took the first available data point with a velocity at  $t=.30919$ . I found the acceleration by taking the derivative of the line of best fit of the velocity. And the change in time I also found from the initial data point by plugging in. I found the velocity at  $t=.5$ .